A conversation with Don Dawson

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Abstract.

Donald Andrew Dawson (Don Dawson) was born in 1937. He received a bachelor’s degree in 1958 and a master’s degree in 1959 from McGill University and a Ph.D. in 1963 from M.I.T. under the supervision of Henry P. McKean Jr. Following an appointment at McGill University as professor for 7 years, he joined Carleton University in 1970 where he remained for the rest of his career. Amongst his many contributions to the theory of stochastic processes, his work leading to the creation of the Dawson-Watanabe superprocess and the analysis of its remarkable properties in describing the evolution in space and time of populations, stand out as milestones of modern probability theory. His numerous papers span the whole gamut of contemporary hot areas, notably the study of stochastic evolution equations, measure-valued processes, McKean-Vlasov limits, hierarchical structures, super-Brownian motion, as well as branching, catalytic and historical processes. He has over 200 refereed publications and 8 monographs, with an impressive number of citations, more than 7 000. He is elected Fellow of the Royal Society and of the Royal Society of Canada, as well as Gold medalist of the Statistical Society of Canada and elected Fellow of the Institute of Mathematical Statistics.

Key words and phrases: Biography, probability, statistics, stochastic processes, physics, biology.

Celebrating 50 years of Stochastics at Carleton University

1. INDIVIDUAL EXPERIENCE

BN et al.: How did you initially get interested in the subject of probability?

Don: In my undergrad days the role of entropy in thermodynamics captured my interest. The use of entropy in information theory and its applications to mathematical linguistics which was the subject of my M.Sc. thesis. Then at M.I.T., as a member of the Artificial Intelligence Project, I was inspired by the course of Marvin Minsky in the new field of artificial intelligence which dealt with the uses of random methods for search and interacting systems. I took an inspiring course on the (now famous) book of Henry P. McKean Jr. and Kiyosi Itô: Diffusion processes and their sample paths (Itô and McKeans, 1974) and decided to write my thesis on this topic.

BN et al.: Who were your mentors during your studies?

Don: At McGill University, Edward Rosenthal whose real analysis course was inspiring. Joachim “Jim” Lambek was the advisor for my M.Sc. thesis, and at M.I.T., my Ph.D. advisor was Henry P. McKean, Jr. I returned to McGill after completing my Ph.D. to take up a professorship. I taught at McGill University from 1963 to 1970 where I had four Ph.D. students. (I had two more at McGill later on.) Then in 1970 I came to Carleton University, where I su-
I supervised 23 Ph.D. students. I also worked with 35 postdoctoral fellows and research associates.

2. EARLY YEARS

BN et al.: You came from McGill to Carleton University in 1970. What were your main motivations and the challenges you faced?

Don: The main motivation was to build the Carleton Ph.D. program. The first challenge was having the assessment of the Ph.D. Program in Probability and Statistics. Fortunately Miklós Csörgő came in 1971 and the two of us worked together, then a couple of years later Jon Rao came.

BN et al.: Talk to us about your early years at Carleton University.

Don: Many activities arose at Carleton during the 1970’s. For example there was the Symposium on Probability and Related Topics in 1973. Another was a series of lectures by Takeyuki Hida on the Analysis of Brownian Functionals in 1975, highlighted throughout by Hida’s signature fans in his overhead talks! Also memorable were a series of lectures by Josef Steinebach on Large deviation probabilities and some related topics in 1980, and the International Symposium in Ottawa in 1980, for which the proceedings were published in 1981 by North-Holland.

BN et al.: How did the collaborations with the University of Ottawa emerge?

Don: At McGill I had developed a close relationship with Anatole Joffe, who had studied with Mark Kac. Anatole’s former student David McDonald and later my student Gail Ivanoff, as well as Mayer Alvo, who came from Columbia University, after a masters thesis at McGill, all became professors at the University of Ottawa. As a result it was normal to have good relations between the two universities.

3. LRSP YEARS

BN et al.: The Carleton University-University of Ottawa Laboratory for Research in Statistics and Probability (LRSP) at Carleton University was a hive of research in probability and statistics from its creation in 1982 on. How did it come about and what were the main challenges to its creation?

Don: The main challenges were to find the appropriate funding. From 1983 to 1998, we obtained over 400K from the Natural Sciences and Engineering Research Council of Canada (NSERC). We also benefited from NSERC Conference grants and International Foreign Researcher grants.

BN et al.: Using rankings based on all research articles published between 1986 and 2000 inclusively in 25 select journals of high reputation (9 in Probability and 16 in Statistics), Genest and Guay
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(2002) identified the Carleton University Statistics and Probability group as one of only two in the world as having high productivity in both statistics and probability (the other one was Cornell), among the top 15 most productive statistical institutions in the world at the time. In a prior survey of the period 1986-1995 by Genest (1999), the LRSP was one of three such groups (the other two were Cornell and the Université Libre de Bruxelles). What was the secret of the success of the LRSP? What are the key ingredients in your opinion?

**Don:** What made the LRSP so successful was the set of people who formed the team and the participation of a critical mass of researchers from Carleton University, the University of Ottawa and Statistics Canada. The key was a wide vision of the discipline of stochastics, and the scientific generosity of its members. The funding we received made possible the hiring of Mrs. Gill Murray as the Coordinator of the LRSP; she provided the outstanding coordination and was the glue which made the wide range of activities possible.

**BN et al.:** Would it be possible to reproduce this success today? What are the barriers to realizing this again?

**Don:** Many things have changed since 1982. It is not clear to me what mechanism could produce this type of funding. However if this were possible, and the other conditions I mentioned above for this success of LRSP were met, it could be achieved.

**BN et al.:** Can you speak to us about the major contributions to our field that emerged around the Laboratory, during that time and since? What was the impact of the numerous visitors on site? Can you name a few of the most distinguished visitors you received at the Laboratory? Any defining moments (conferences or visits) or anecdotes (amusing or enlightening) to share with us?

**Don:** Our Technical Report Series was a real success with more than 450 volumes. Over the course of 50 or so years there are many enlightening and sometime amusing incidents involving visitors. I can highlight a few.

One of the most inspiring talks was given by Mark Kac, who was one of the first to explain mathematical physics and the Gibbs measure to probabilists like me. One of his favorite saying was “a demonstration convinces a reasonable man whereas a proof satisfies a stubborn one”.

Robert Adler (1989) who was used to the weather in Australia and Israel, faced a -30 degree (C) spell in Ottawa. He looked a little cold but it did not affect his impressive presentation. This included a lab demonstration of his software which later appeared as “Superprocesses - The Movie”.

Jean-Francois Le Gall’s blackboard talks, given as part of the Fields Institute thematic program on Probability and its Applications in August 1998 - July 1999, were both inspiring and enlightening.

As time went by mathematics talks went from blackboard to overhead slides and then to computer aided talks. A case in point were the superb lectures Tom Kurtz gave on the “look-down” process about his work with Peter Donnelly (Donnelly and Kurtz, 1996). This became one of the major advances in population genetics. His lecture was an excellent example of the good use of a computer talk. Another memorable lecture was given by Terry Lyons on his seminal work introducing rough paths. Terry’s was the first one I saw using a computer (tablet) as a “blackboard”.

**FIG 3. Don Dawson and Gill Murray**

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4. COLLABORATIONS AND INTERACTIONS

BN et al.: What are your favorite papers and why?

Don: I have listed my 3 favorite papers before 1991 because my future work, one way or another, was based on these three.

Dawson and Hochberg (1982) is a favorite of mine since it led to much of my research since then that has been focused on Fleming-Viot processes. Wendell Fleming was the External Examiner for Amit Bose’s Ph.D. thesis defense in 1977 and he came to Carleton for this reason. We discussed his joint work with Viot and I became interested in their model. Ken Hochberg came to Carleton as a PDF (he was also supervised by H.P. McKean). With Ken we saw that we could show that the moment measures satisfies de Finetti’s Theorem and to use this to reconstruct the measure. One application was to show that the long time behavior has a coherence property called which we called “wandering”. I gave a talk at the Annual Winter Meeting of the Canadian Mathematical Society at Vancouver in December 1980 on an early draft and somebody pointed out the connection that our wandering measure could be interpreted as a continuous limit of the model of Kingman (1976). This also led to Dawson and Hochberg (1983).

Dawson and Gärtner (1987) is also a favorite of mine since it was a starting point for future applications of large deviation arguments in mean-field models. I first met Jürgen in Berlin in 1986 while visiting Klaus Fleischmann. I was interested in McKean-Vlasov processes (Dawson, 1983) and Jürgen was an expert on large deviation theory. The purpose of this paper was to show that the numbers of particles $N \to \infty$ which is given by the McKean-Vlasov equation and the large deviation behavior is described by a generalization of the Freidlin and Wentzell results to obtain a characterization of the action functional. This is achieved by a projective limit of large deviation systems, large deviations on dual vector spaces, and a Sanov type theorem for vectors of empirical measures. I co-authored several papers with Jürgen including a AMS memoir and lectures at the Cambridge Symposium in 1987, ‘Stochastic calculus in application’. I learned a great deal from him. Based on Google searchers there were a surprising numbers of citations on mean-field results and their large deviations limits as the number of particles goes to $\infty$. This includes stochastic dynamic games, stochastic filtering, stochastic control, stochastic spin systems, ecology, non-equilibrium thermodynamics and random polymers.

Another favorite of mine is Dawson and Perkins (1991) since it brought together the work done on superprocesses during the period 1968 and 1990 by Watanabe, Iscoe, Perkins and me by introducing the historical processes as a superprocess which is enriched to contain information on the genealogy of the population.

BN et al.: How did historical processes come about? You co-wrote major papers on the subject with Ed Perkins. Can you speak in more detail about this collaboration?

Don The subject began with Watanabe (1968). Unfortunately, I was unaware of this article until I read Walsh’s Saint-Flour notes (Walsh, 1986) which refers to it. My work on superprocesses was originally motivated by the dimensional dependence of stochastic evolution equations in Euclidean spaces (Dawson, 1972, 1975). In my 1975 paper, the stochastic evolution equation on branching results in a measure-valued process in any dimension. This is based of the use of the Trotter product formula. Dawson (1977, 1978, 1979), Dawson and Hochberg (1982), those of Iscoe (1981, 1986a,b, 1988) (who had developed a formula for the occupation time of a superprocess in his Carleton Ph.D. thesis) and Perkins (1988, 1989, 1990) also explore many questions of the dimension dependence.

The notion of the historical process came about in early discussions we had with Ian Iscoe. The formulations of historical processes that took place in the sixth floor of the Dunton Tower at Carleton University slowly came together using the general superprocess due to Fitzsimmons, the use the nonstandard characterization of weak convergence, which was new to me, and the Palm measure formula and Campbell measure. The latter was based on the theory of infinitely divisible random measures of Jagers (1974), Kallenberg (1977), Matthes et al. (1978).
Over the next fifteen years I had the pleasure to work on several projects with Ed. One example of this is our joint work on mutually catalytic branching. During that time we were stuck on finding the dual - fortunately Leonid Mytnik produced new dual. In turn this led to the five author collaboration Dawson et al. (2002). One memorable meeting of the authors was at the Fields Institute. Over the years Perkins has made the many of the deepest results in superprocess. His Saint-Flour Notes Perkins (2002) contain the state of the art before 2003. I have been also influenced in particular by his later joint work with Steve Evans (Evans and Perkins, 1998). This, together with Barlow and Perkins (1994), played an important role in Dawson and Fleischmann (1997).

BN et al.: Can you talk to us about your relationship over the years with Dynkin and Le Gall? The publications by Dynkin and Le Gall in the field came much later and the main ones are both dated in 1991. What can you say about their contribution to our understanding of superprocesses and how superprocesses came to bear your name, as in Dawson-Watanabe processes?

Don: In the late 1980’s Dynkin became interested in superprocesses. I first leaned of this by an email message asking questions about my 1978 paper. Later he also arranged a visit by me and also Iscoe to Cornell. I was invited to give one of the Barrett lectures at the University of Tennessee in 1993. Dynkin was one of the other lectures there where I learned of his new results; these also formed the contents of Dynkin (1994). Over the years Dynkin made many contributions to superdiffusions including the important notion of branching exit Markov systems. This and many more deep results of his are presented in Dynkin (2002). Dynkin’s branching rate functional played an essential role in Dawson and Fleischmann (1997). Dynkin introduced the name superprocesses in Dynkin (1988) and the name Dawson-Watanabe processes in the book Dynkin (1994). He later introduced the class of superprocesses \((\xi, K, \psi)\). The superprocess with \(\xi\) a Brownian motion, quadratic branching and \(K(t) \propto dt\) was called the Dawson-Watanabe superprocess.

Le Gall presented his Brownian excursion, trees and measure-valued branching processes paper (Le Gall, 1991) at the Workshop on Infinite dimensional Markov processes at Cornell University in May 1989. This paper develops a representation based on a tree inspired by Neveu and its relation to the historical process. It is a powerful tool for the superprocess and their generalizations. His basic construction is extended in Duquesne and Le Gall (2002) to Lévy processes to produce the Lévy snake. One application is to get the stable analogue of Aldous’ continuum Brownian random tree (Aldous, 1991a,b, 1993). The Brownian snake also was used in the Habilitation Dissertation of J-F Delmas, for which I was asked to report in 1997. It included a section on catalytic branching including his paper with Fleischmann. His work has influenced me in several ways. In 2002 we used the Brownian snake to discuss strong clumping in a stable catalytic medium (Dawson et al., 2002). Also the stochastic flow results of Bertoin and Le Gall (2003), Bertoin and Le Gall (2005) were the inspiration for Dawson and Li (2012).

BN et al.: Other than Dynkin, Le Gall and Perkins, which three other researchers would you consider to have written the most influential papers in your field or fields of endeavour? How did they influence your own research?

Don: I will mention Allison Etheridge, Tom Kurtz and Tokuzo Shiga. Barton et al. (2010) was the beginning of an approach to evolution in a spatial continuum that has since had an important impact on the subject. Etheridge (2011) and subsequent work since is a major contribution to evolutionary biology. I have followed the work of Etheridge since her Ph.D. thesis. Etheridge and March (1991) was the first to point out the relationship between superprocesses and the Fleming-Viot process which was an important step. We were co-authors on Dawson et al. (2002).

Donnelly and Kurtz (1996) was the start of a development which represents the genealogy of a Fleming-Viot populations and it had a major impact on population biology. I spent my sabbatical during 1980-1981 visiting the University of Wisconsin. Kurtz and his former student Ethier were starting to work on Etheridge and Kurtz (1986) which has
had a major impact in the field of Markov Processes. At that time I was completing the joint paper with Ken Hochberg on the Fleming-Viot process which had introduced the dual method for measure-valued processes. In a train ride from Madison to Chicago we started to work on our joint paper on the general conditions necessary for the duality. Greven and I used the results of Ethier-Kurtz and especially the results on coupling and ergodic theorems.

I spent the period Oct-Nov 1994 visiting Shiga at the Tokyo Institute of Technology and learned much from him. I was familiar with his earlier paper Shiga and Shimizu (1980) on infinite-dimensional stochastic differential equations, when he gave a series of lectures at Carleton, up to Konno and Shiga (1988). But I was unaware of his earlier work (Shiga and Uchiyama, 1986) which I learned during this visit. This paper provided some of the key tools in my later work with Greven on Fleming-Viot processes (Dawson and Greven, 1999, 2014).

**BN et al.:** Can you talk to us about your relationship over the years with your long term collaborators Klaus Fleischmann, Luis Gorostiza, and Andreas Greven?

**Don:** I first met Klaus Fleischmann at a meeting in Hungary in 1978. We had a long collaboration. We worked on catalytic and mutually catalytic super-Brownian motions, including the work mentioned previously. Among my favorites is Dawson and Fleischmann (1997).

Luis Gorostiza is another one of my long term collaborators. Our first joint paper was in 1984 (Dawson and Gorostiza, 1984). We worked on a variety of topics, including Dawson et al. (2002), and Dawson et al. (2001) where, among other things, we identify the order of transience and recurrence of hierarchical processes. Most recently, we worked on random walks and percolation on Euclidean and hierarchical systems and their continuum limits (Dawson and Gorostiza, 2018). Highlights were our trips to Beijing and CIMAT in Guanajuato.

If the metric is number of pages published together, then Andreas Greven and I are definitely the closest of collaborators! My collaboration in the early years with Andreas started with a Colloquium he gave at Carleton on his joint work with Ted Cox (Cox and Greven, 1994), and discussions we had afterwards. In 1995 at Carleton we collaborated with Jean Vaillancourt on equilibria and quasiequilibria for infinite systems of interacting systems Fleming-Viot processes (Dawson et al., 1995). From May to July 2001 I was the Otto Haupt Visiting Professor at the University of Erlangen-Nürnberg and I had the pleasure to give a class to Greven’s graduate students. In the last 20 years Greven and his students Achim Klenke, Peter Pfaffelhuber and Anita Winter had produced deep results on superprocesses and their generalizations. In 2008 at EURANDOM, we studied the renormalization transformation for two type branching models (Dawson et al., 2008). Our work on Fleming-Viot models with selection and mutation culminated with Dawson and Greven (2014). This constructed a rigorous framework for the analy-
sis of the evolution of population toward fitter types though punctuated equilibria. We also taught a joint minicourse in 2017 based on this book at EURANDOM.

**5. SCIENTIFIC CONTRIBUTIONS**

**BN et al.:** You have published more than 200 papers. Many of your contributions aim at describing and analyzing the behavior of branching particle systems. Can you describe for our readers how your interest for these arose?

**Don:** This arose out my interest in the theory of the stochastic heat equation

\[ \frac{\partial X}{\partial t} = \frac{\partial^2 X}{\partial x^2} + \alpha X^\beta \frac{\partial B}{\partial t} \]

with \( \beta \in (0, 1] \) and \( B(t) \) is standard Brownian motion. The case \( \beta = \frac{1}{2} \) represents continuous state branching. The starting point was Dawson (1972) in which existence and uniqueness for Hilbert-space valued solutions for a class of parabolic stochastic partial differential equations (SPDE) with Lipschitz coefficients and the joint continuity in space and time for the stochastic heat equation in one dimension were established. In Dawson and Salehi (1980) it was noted that the linear SPDE \( dX(t, x) = \Delta X(t, x) + (X(t, x))^1/2 W(dt, dx) \), where \( W(\cdot, \cdot) \) denotes space-time white noise, does not have a function-valued solution but does have a measure-valued solution. This problem was addressed in Dawson (1975) by reformulating it as a measure-valued process for which existence and uniqueness in law was established. The resulting process now known as super-Brownian motion or Dawson-Watanabe superprocess had also been discovered earlier by S. Watanabe in the context of continuous state branching processes.

**BN et al.:** Your work on branching particle systems led to the introduction of families of measure-valued processes, which grew into a whole new field within probability theory. What are the results you are most proud of in this area?

**Don:** During the years 1970-1995 my research program focussed on the characterization and classification of basic classes of measure-valued processes and the study of the small spatial scale and large space-time scale behavior of these processes. This led to the systematic development of the foundations of measure-valued processes presented in Dawson (1993, 2017) which now have important applications in genetics, ecology and other fields. For other measure-valued processes whose states are not infinitely divisible random measures, dual representations, that had applications to infinite particle systems, also could be applied to some measure valued processes. In Dawson and Hochberg (1982) we developed the method of duality for the probability measure-valued processes introduced by Fleming and Viot, as well as a particle representation and decomposition into a tree of subfamilies. Duality was also a key ingredient in a joint paper with George Papanicolaou (Dawson and Papanicolaou, 1984) for a Hilbert space-valued random Schrödinger process. The duality method was also reformulated in an abstract setting in a joint paper with Tom Kurtz (Daw-
son and Kurtz, 1982) and this has now become a standard tool.

Another basic tool is the historical superprocess and its canonical representation which we introduced in a joint paper with E.A. Perkins (Dawson and Perkins, 1991) and used there to establish a number of structural properties of super-Brownian motion including the clan decomposition of the equilibrium distribution.

A method that can be used to handle a class of nonlinear interactions is the Dawson-Girsanov formula for measure-valued processes that we derived in Dawson (1978) and has been used to incorporate selection in Fleming-Viot processes and nonlinear birth and death rates in superprocesses. Some results for nonlinear sampling rates for Fleming-Viot sufficiently close to constant rates were obtained in a joint paper with P. March (Dawson and March, 1995) using a class of resolvent estimates and a semigroup perturbation argument.

BN et al.: What were the main applications driving the research on measure-valued processes?

Don: The are so many applications. Here are a few.

Catalytic and mutually catalytic processes:
A catalytic particle system is one in which the reactant population produces new particles only in the presence of a catalyst. A class of catalytic superprocesses was introduced and studied in a series of joint papers with Klaus Fleischmann. An example of that is Dawson and Fleischmann (1997) where a super-Brownian motion is catalyzed by another super-Brownian motion which is non-degenerate only in dimensions \( d = 1, 2, 3 \). Similar analysis can be carried out for catalytic chains having no cycles but chains having cycles are fundamentally different. The case of a 2-cycle (mutually catalytic branching) in which each of two types catalyzes the production of the other was introduced in Dawson and Perkins (1998). In the case of one spatial dimension existence and weak uniqueness was obtained with E.A. Perkins (Dawson and Perkins, 1998) for the associated pair of SPDE. Existence and uniqueness in law for the corresponding martingale problem in \( R^2 \) was established in a series of three papers in collaboration with A. Etherridge, K. Fleischmann, L. Mytnik, E.A. Perkins and J. Xiong but remains an open problem for \( d \geq 3 \).

Analysis of interacting systems in large space and time scales: A central problem in both statistical physics and population biology is the determination of the long-time behaviour and possible equilibrium states for interacting systems on the lattice \( Z^d \) (or other spatial network topology) with homogeneous initial conditions. We developed a program to determine such behavior for interacting diffusions, superprocesses, catalytic systems Cox et al. (2004) and interacting Fleming-Viot processes (Dawson and Hochberg, 1982) and developed methods for this purpose including McKean-Vlasov limit dynamics, large deviations for measure-valued processes and the hierarchical mean-field limit.

Large scale structures in measure-valued processes: Dawson (1977) resolved the problem of the existence of spatially homogeneous equilibria for critical branching systems in \( \mathbb{R}^d \) by identifying a dichotomy in which local extinction and the formation of rare clumps occurs in dimensions \( d = 1, 2 \) and non-trivial equilibria exist in dimensions \( d \geq 3 \). Dawson and Perkins (1998) establishes the same dichotomy for the mutually catalytic system on the lattice \( \mathbb{Z}^d \), Dawson and Greven (1999) establishes this for the interacting Fleming-Viot system and Dawson et al. (2004) for multilevel branching (but with critical dimension \( d = 4 \)).

Mean-field methods and large deviations: Finally, mean-field models are used to capture major features of the behaviour such as the phase transition structure. They arise in the McKean-Vlasov limit of a measure-valued system in which the spatial interaction is replaced by N exchangeably interacting systems and then analysing the \( N \to \infty \) limit. An application of mean-field methods to queueing systems is given in Dawson et al. (2005). In Dawson (1983) we used the limiting McKean-Vlasov dynamics to study phase transitions, critical slowing down and the emergence of non-Gaussian fluctuations at the critical point. The study of the large deviations for interacting systems and measure-valued processes was initiated in a
series of joint paper with Jürgen Gärtner. This was used in Dawson and Gärtner (1987) to derive Wentzell-Freidlin estimates for deviations from the McKean-Vlasov limit in order to investigate the transition between quasi-equilibria in large finite systems. Large deviation methods are used in Dawson-Feng, including Dawson and Feng (2006), to study asymptotics for the Fleming-Viot process in the infinite population limit.

**BN et al.:** What do you see as future applications or problems for measure-valued processes?

**Don:** Several show intense research activity as we speak: mean field games and spatial mean field games, spatial epidemic models, ecology and evolutionary biology, multilevel systems, hierarchical network theory, random wave propagation, affine processes in finance.

**BN et al.:** Much of your later research production is concerned with applications to evolutionary biology. Tell us about hierarchical particle systems you and your collaborators introduced in order to model these extremely complex phenomena.

**Don:**

**Hierarchical analysis and the degree of random walks:** Hierarchical systems play a role in many fields such as evolutionary biology, neuroscience, protein dynamics, statistical physics, and Bayesian statistics. Our research on this began jointly with Andreas Greven (Dawson and Greven, 1993). In turn, this led to our interest in the potential theory of random walk on groups in which we introduced the notion of degree of random walks. The results on branching on the hierarchical group based on the degree of random walks joint research are presented with Luis Gorostiza and Anton Wakolbinger (Dawson et al., 2001).

Hierarchical mean-field analysis on the hierarchical group was introduced in joint work with Andreas Greven (Dawson and Greven, 1993, 1999), and used to study interacting systems including branching systems, interacting Fleming-Viot processes (Dawson and Greven, 1999) and catalytic systems (Cox et al., 2004) in multiple space and time scales and their dependence of the degree of the underlying random walk.

This research program has the objective of proving that the large scale behaviour of spatially interacting systems can be classified into a small number of universality classes (Dawson et al., 2008).

**Application to evolutionary biology and ecology:** Evolutionary biology is based on a complex adaptive system in which reproduction of individuals, subject to mutation and selection located on a space of sites, combine with migration between sites, given by a random walk in a spatial environment. This can be modelled by spatial Fleming-Viot systems with mutation and selection on a fitness landscape with its ultrametric structure. We consider, in particular, the emergence of new species. The analysis of this system and its behaviour in the long time scales involved, made it necessary to find a new family of dual processes, the set-valued ones. This was carried out in the book with Andreas Greven (Dawson and Greven, 2014).

Much current interest has developed in recent years in the question of levels of selection in evolutionary biology and evolutionary ecology. The corresponding natural framework for multilevel multitype models with random effects at different levels is the setting of multilevel measure-valued processes. In particular two-level measure-valued processes have state spaces of the form $\mathcal{M}(\mathcal{M}(E))$ for some Polish space $E$ where $\mathcal{M}(E)$ denotes the space of Borel measures on $E$. In Dawson (2018) we work with an analogous class of two level probability measure-valued processes formulated in terms of a well-posed martingale problem which generalizes the two-type model to systems with more than two types, more complex interactions and to the diffusion limit of systems with finitely many sites. The application of this framework to evolutionary biology and ecology of multi-species systems in which the fitness of a species can depends on the higher level distributions of related species is given in Dawson (2018).

The problem of extending this analysis to spatially random environments modelled by migration between sites given by a nearest neighbour random walk on a network of long-range percolation clusters. This was recently carried out in ultrametric spaces in joint research with Luis Gorostiza (Dawson and Gorostiza, 2018).
6. ACADEMIC DUTIES

BN et al.: How did you reconcile this prolific productivity with your heavy involvement in editorial duties, directorships, grant agencies committee work, etc.?

Don: My main responsibilities were Department Chair (1974-1977), Co-Editors-In-Chief of the Canadian Journal of Mathematics (1988-1993), 5 terms of NRC and NSERC committees during 1974-1995, Director of the Fields Institute (1996-2000) and President of the Bernoulli Society (2003-2005). During many of these years my graduate students and co-authors kept me alive scientifically.

BN et al.: During your presidency of the Bernoulli Society, can you identify one or two key events of note to the community that you had a hand in?

Don: Three events do stand out. First is the 6th Bernoulli-IMS World Congress in Probability and Statistics, held in Barcelona in 2004. There were great plenary lectures by Jun Liu, Steffen L. Lauritzen, David Aldous, Wendelin Werner, Iain Johnstone, Peter Bickel, Vladimir Koltchinskii, Evarist Giné, Cun-Hui Zhang, Alison Etheridge, and Dominique Picard. Quite a roster! This was followed by an excellent European Meeting of Statisticians in Oslo (2005). Last but not least, the agreement with the IMS called “Joined-up Thinking”, the creation of a joint Bernoulli Society/IMS membership beginning in 2005. It seems natural now, given that the two societies share common objectives, namely the advancement of probability and statistics and their applications.

BN et al.: What is the role of your colleagues, friends, and family in your professional successes?

Don: My wife Elizabeth (Betty) and children Michael and Suzanne have made everything possible. My colleagues, my students, my co-authors and visitors provided the environment which were instrumental to my research program. I owe my co-authors a special thanks.

7. PROSPECTIVE QUESTIONS

BN et al.: Where do you see the field heading?

Don: Randomness is ubiquitous and has produced many diverse many manifestations. Examples arise in the analysis of probabilistic models for real-world phenomena from physics, biology, neuroscience, statistics, and computer science. Some specific topics of current interest are: statistical physics in a random environment, random matrix theory, branching systems in biology, random energy landscapes, data structure analysis, genetics and population biology, stochastic partial differential equations, networks and random walks on random graphs.

BN et al.: What do you see as the future of probability in the world of Artificial Intelligence and Big Data?

Don: These fields are multidisciplinary and require team work. This includes probability which is involved in hierarchical Bayes networks, random search, random landscapes, statistical physics and deep learning algorithms in data sciences.
BN et al.: What is your assessment of the current state of health of the field of stochastics in Canada and around the world?

Don: Stochastics has been developed in many directions over the past 50 years and is still going strong. Canada plays an important role in several areas and LRSP itself has contributed much to this success. Stochastics continues to generate important gains in health science, social science, economics, physics, genetics, evolutionary biology, neuroscience, interacting systems and networks, analysis of algorithms, financial probability and our general scientific knowledge on the whole.

BN et al.: Do you have any advice for the young researcher in probability.

Don: Develop your set of mathematical skills. This can provide a foundation in future years as you broaden your interests. Keep your eyes open for new opportunities, for new applications, and for scientific cooperation.

The interested reader can find out more by going to http://dynkincollection.library.cornell.edu/node/954

REFERENCES


